

Ex.1-1, Prob.3-35 (HRW,8e) *Sol.*

We apply Eq. 3-30 and Eq. 3-23. If a vector-capable calculator is used, this makes a good exercise for getting familiar with those features. Here we briefly sketch the method.

(a) We note that $\mathbf{b} \times \mathbf{c} = -8.0\mathbf{i} + 5.0\mathbf{j} + 6.0\mathbf{k}$. Thus, $\mathbf{a} \cdot \mathbf{b} \times \mathbf{c} = (3.0)(-8.0) + (3.0)(5.0) + (-2.0)(6.0) = -21$.

(b) We note that $\mathbf{b} + \mathbf{c} = 1.0\mathbf{i} - 2.0\mathbf{j} + 3.0\mathbf{k}$. Thus, $\mathbf{a} \cdot (\mathbf{b} + \mathbf{c}) = (3.0)(1.0) + (3.0)(-2.0) + (-2.0)(3.0) = -9.0$.

(c) Finally, $\mathbf{a} \times (\mathbf{b} + \mathbf{c}) = [(3.0)(3.0) - (-2.0)(-2.0)]\mathbf{i} + [(-2.0)(1.0) - (3.0)(3.0)]\mathbf{j} + [(3.0)(-2.0) - (1.0)(3.0)]\mathbf{k} = 5.0\mathbf{i} + -11\mathbf{j} - 9.0\mathbf{k}$.

Ex.1-2, Prob.3-38 (HRW,8e) *Sol.*

The displacement vectors can be written as

$$\mathbf{d}_1 = (4.50 \text{ m})(\cos 63^\circ \mathbf{j} + \sin 63^\circ \mathbf{k}) \\ = (2.042 \text{ m} \mathbf{j} + 4.009 \text{ m} \mathbf{k}),$$

$$\mathbf{d}_2 = (1.40 \text{ m})(\cos 30^\circ \mathbf{i} + \sin 30^\circ \mathbf{k}) \\ = (1.212 \text{ m} \mathbf{i} + 0.700 \text{ m} \mathbf{k}).$$

(a) The dot product of \mathbf{d}_1 and \mathbf{d}_2 is

$$\mathbf{d}_1 \cdot \mathbf{d}_2 = (2.042 \mathbf{j} + 4.009 \mathbf{k}) \cdot (1.212 \mathbf{i} + 0.700 \mathbf{k}) \\ = (4.009 \mathbf{k}) \cdot (0.700 \mathbf{k}) = 2.806 = 2.81 \text{ (m}^2\text{)} \text{ or} \\ \text{Ans. } 2.81 \text{ m}^2.$$

(b) The cross product of \mathbf{d}_1 and \mathbf{d}_2 is

$$\mathbf{d}_1 \times \mathbf{d}_2 = (2.042 \mathbf{j} + 4.009 \mathbf{k}) \times (1.212 \mathbf{i} + 0.700 \mathbf{k}) \\ = (2.042) \times (1.212) (-\mathbf{k}) + (2.042) \times (0.700) \mathbf{i} + \\ (4.009)(1.212) \mathbf{j} = (1.429 \mathbf{i} + 4.858 \mathbf{j} - 2.474 \mathbf{k}) \\ = (1.43 \mathbf{i} + 4.86 \mathbf{j} - 2.47 \mathbf{k}) \text{ (m}^2\text{)} \text{ or} \\ \text{Ans. } (1.43 \mathbf{i} + 4.86 \mathbf{j} - 2.47 \mathbf{k}) \text{ m}^2.$$

(c) The magnitudes of \mathbf{d}_1 and \mathbf{d}_2 are

$$|\mathbf{d}_1|^2 = 20.24, |\mathbf{d}_1| = 4.500, |\mathbf{d}_2|^2 = 1.959, |\mathbf{d}_2| = 1.400, \\ \text{Thus, the angle between the two vectors is} \\ \theta = \cos^{-1} [|\mathbf{d}_1 \cdot \mathbf{d}_2| / (d_1 d_2)] \\ = \cos^{-1} [2.806 / (4.500 \times 1.400)] = \cos^{-1} (0.4454) \\ = 63.55^\circ \approx 63.6^\circ.$$