

Chapter 30 (Benson)

E01 $F = \mu_0 I_1 I_2 bc / 2\pi a(a + b)$.

E06 $F = \mu_0 I_1 I_2 / 2\pi d$: $F_{38} = 80 (\mu\text{N/m})$, $F_{36} = 60 (\mu\text{N/m})$. $F_x = (F_{38} + F_{36}) \cos 60^\circ = 70 (\mu\text{N/m})$; $F_y = (F_{38} - F_{36}) \sin 60^\circ = 17.3 (\mu\text{N/m})$.

E09 $B = (\mu_0 I / 2a) / 2 + 2(\mu_0 I / 4\pi a) = (\mu_0 I / 2a)(1/2 + 1/\pi)$, out.

E10 $B = \mu_0 I / 2a + \mu_0 I / 2\pi a = (\mu_0 I / 2a)(1 + 1/\pi)$, out of page.

E11 $B = \mu_0 I / 4a - \mu_0 I / 4b = (\mu_0 I / 4)(1/a - 1/b)$, into page.

E22 $B_{cir} = \mu_0 I / 4a$, $B_h = (\mu_0 I / 8\pi a)(2 \sin \alpha_1)$, $B_v = 2(\mu_0 I / 4\pi a)(\sin \alpha_2)$, where $\sin \alpha_1 = 1/\sqrt{5}$, $\sin \alpha_2 = 2/\sqrt{5}$. $B = (\mu_0 I / a)(1/4 + 1/\pi\sqrt{5} + 1/4\pi\sqrt{5})$.

E23 (a) $B = (\mu_0 I / 4)(1/a + 1/b) = 3.14 \times 10^{-5} \text{ T}$;

(b) $\mu = IA = I\pi(a^2 + b^2) = 0.254 \text{ A}\cdot\text{m}^2$.

E27 $\oint \vec{B} \cdot d\vec{l}$ is not zero, even though $I = 0$.

E32 \vec{B} is normal to $d\vec{l}$ for the radial sections. For circular arcs:

$$\int \vec{B} \cdot d\vec{l} = (\mu_0 I / 2\pi a)(\pi a / 2) + (\mu_0 I / 2\pi b)(3\pi b / 2) = \mu_0 I$$

E42 $F_{12} = \mu_0 I_1 I_2 / 2\pi r$. $F_x = \mu_0 I^2 / 2\pi d - \mu_0 I^2 \cos 45^\circ / 2\pi\sqrt{2}d = \mu_0 I^2 / 4\pi d$, $F_y = -\mu_0 I^2 / 2\pi d - \mu_0 I^2 \cos 45^\circ / 2\pi\sqrt{2}d = -3\mu_0 I^2 / 4\pi d$. With $d = 5 \text{ cm}$ & $I = 8 \text{ A}$, $\vec{F} = (1.28 \hat{i} - 3.84 \hat{j}) \times 10^{-4} \text{ N/m}$.

P01 $I = q/T = qv / 2\pi R$; $mv^2 / R = qvB$, or $v = qRB / m$; Thus $I = q^2 B / 2\pi m$ $B = \mu_0 I / 2a = \mu_0 q^2 B / 4\pi m R$. (Teacher: Jyh-Shinn Yang, 89.06.03)

P02 (a) $B = (\mu_0 N I R^2 / 2)([R^2 + (R/2 + x)^2]^{-3/2} + [R^2 + (R/2 - x)^2]^{-3/2})$;

(b) As $x = 0$, $B = \mu_0 N I (4/5)^{3/2}$.

P09 The field due to an infinite cylinder inside it is $\vec{B} = \mu_0 I \vec{r} / 2\pi R^2$, where \vec{r} is position vector from the axis. For a long, solid wire containing a cavity of radius a can be treated as the superposition of a completely solid wire and a wire of radius a carrying a current in the opposite direction. Therefore, the field in the cavity is $\vec{B} = (\mu_0 I / 2\pi R^2)(\vec{r}_1 - \vec{r}_2)$, where \vec{r}_1 and \vec{r}_2 are the position vectors from the axes of the solid wires with radii R and a , respectively. Thus $\vec{B} = (\mu_0 I / 2\pi R^2)\vec{d}$, uniform in the cavity.